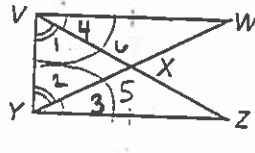


Given:  $\angle ZVY \cong \angle WYV$  (1) (2)  
 (4)  $\angle ZVW \cong \angle WYZ$ , (3)  
 $\overline{VW} \cong \overline{YZ}$   
 Prove:  $\Delta ZVY \cong \Delta WYV$

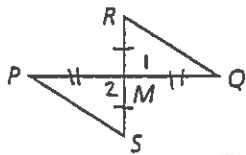


- |                                       |                          |
|---------------------------------------|--------------------------|
| ① $\angle 1 \cong \angle 2$           | ① given                  |
| ② $m\angle 1 = m\angle 2$             | ② def of $\cong$         |
| ③ $\angle 3 \cong \angle 4$           | ③ given                  |
| ④ $m\angle 3 = m\angle 4$             | ④ def of $\cong$         |
| ⑤ $m\angle 1 + m\angle 4 = m\angle 6$ | ⑤ angle add. post.       |
| ⑥ $m\angle 2 + m\angle 3 = m\angle 5$ | ⑥ angle add. post.       |
| ⑦ $m\angle 1 + m\angle 4 = m\angle 5$ | ⑦ subst. prop of =       |
| ⑧ $m\angle 6 = m\angle 5$ (st. 5+7)   | ⑧ subst. prop of =       |
| ⑨ $\angle 6 \cong \angle 5$           | ⑨ def of $\cong$         |
| ⑩ $\overline{VY} \cong \overline{VY}$ | ⑩ reflex prop of $\cong$ |
| ⑪ $\overline{VW} \cong \overline{YZ}$ | ⑪ given                  |
| ⑫ $\Delta ZVY \cong \Delta WYV$       | ⑫ SAS                    |

\* note:  
 could also be done  
 with SAS  
 leaving out step 10.

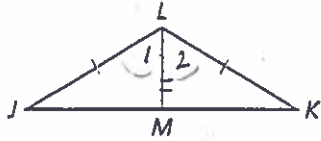
Given:  $M$  is the midpoint of  $\overline{PQ}$  and  $\overline{RS}$ .

Prove:  $\overline{QR} \cong \overline{PS}$



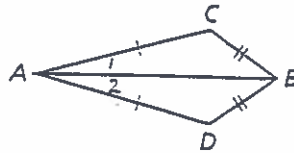
- |  |                            |
|--|----------------------------|
| ① $M$ is the m.p. of $\overline{PQ}$ & $\overline{RS}$ | ① given                    |
| ② $\overline{RM} \cong \overline{MS}$                  | ② def of m.p.              |
| ③ $\overline{PM} \cong \overline{MQ}$                  | ③ def of m.p.              |
| ④ $\angle 1 + \angle 2$ vert. $\angle$ 's              | ④ def of vert. $\angle$ 's |
| ⑤ $\angle 1 \cong \angle 2$                            | ⑤ vert. $\angle$ thm       |
| ⑥ $\Delta SMP \cong \Delta RMQ$                        | ⑥ SAS                      |
| ⑦ $\overline{QR} \cong \overline{PS}$                  | ⑦ c.p.c.t.c                |

Given:  $\overline{LM}$  bisects  $\angle JLK$ .  $\overline{JL} \cong \overline{KL}$   
 Prove:  $M$  is the midpoint of  $\overline{JK}$ .



- |  |                            |
|--|----------------------------|
| ① $\overline{LM}$ bisects $\angle JLK$ | ① given                    |
| ② $\angle 1 \cong \angle 2$            | ② def of $\angle$ bisector |
| ③ $\overline{JL} \cong \overline{KL}$  | ③ given                    |
| ④ $\overline{LM} \cong \overline{LM}$  | ④ reflexive prop $\cong$   |
| ⑤ $\triangle JML \cong \triangle KML$  | ⑤ SAS                      |
| ⑥ $\overline{JM} \cong \overline{MK}$  | ⑥ cpctc                    |
| ⑦ $M$ is the m.p. of $\overline{JK}$   | ⑦ def of m.p.              |

Given:  $\overline{AC} \cong \overline{AD}$ ,  $\overline{CB} \cong \overline{DB}$   
 Prove:  $\overline{AB}$  bisects  $\angle CAD$ .



- |  |                            |
|--|----------------------------|
| ① $\overline{AC} \cong \overline{AD}$  | ① given                    |
| ② $\overline{CB} \cong \overline{DB}$  | ② given                    |
| ③ $\overline{AB} \cong \overline{AB}$  | ③ reflex prop $\cong$      |
| ④ $\triangle CAB \cong \triangle DAB$  | ④ SSS                      |
| ⑤ $\angle 1 \cong \angle 2$            | ⑤ cpctc                    |
| ⑥ $\overline{AB}$ bisects $\angle CAD$ | ⑥ def of $\angle$ bisector |