

STUDY GUIDE: REVIEW, PAGES 202-205

- alternate interior angles
- skew lines
- transversal
- point-slope form
- rise; run

LESSON 3-1

- Possible answer: \overline{DE} and \overline{BC} are skew.
- Possible answer: $\overline{AB} \parallel \overline{DE}$
- Possible answer: $\overline{AD} \perp \overline{DE}$
- Possible answer: plane $ABC \parallel$ plane DEF
- ℓ ; alt. int. \triangleq
- n ; corr. \triangleq
- ℓ ; same-side int. \triangleq
- m ; alt. ext. \triangleq

LESSON 3-2

- $x + 90 = 180$
 $x = 90$
 $m\angle WYZ = x^\circ = 90^\circ$
- $26x + 22 = 38x - 14$
 $22 = 12x - 14$
 $36 = 12x$
 $3 = x$
 $m\angle KLM = 38x - 14$
 $= 38(3) - 14$
 $= 100^\circ$
- $33x + 35 = 26x + 49$
 $7x + 35 = 49$
 $7x = 14$
 $x = 2$
 $m\angle DEF + (26x + 49) = 180$
 $m\angle DEF + 26(2) + 49 = 180$
 $m\angle DEF + 101 = 180$
 $m\angle DEF = 79^\circ$
- $17x + 8 = 13x + 24$
 $4x + 8 = 24$
 $4x = 16$
 $x = 4$
 $m\angle QRS = 13x + 24$
 $= 13(4) + 24$
 $= 76^\circ$

LESSON 3-3

- $\angle 4 \cong \angle 6$, so $c \parallel d$ by the Conv. of the Alt. Int. \triangleq Thm.
- $m\angle 1 = (23x + 38)^\circ = 23(3) + 38 = 107^\circ$
 $m\angle 5 = (17x + 56)^\circ = 17(3) + 56 = 107^\circ$
 $\angle 1 \cong \angle 5$, so $c \parallel d$ by the Conv. of the Corr. \triangleq Post.
- $m\angle 6 = (12x + 6)^\circ = 12(5) + 6 = 66^\circ$
 $m\angle 3 = (21x + 9)^\circ = 21(5) + 9 = 114^\circ$
 $m\angle 6 + m\angle 3 = 66^\circ + 114^\circ = 180^\circ$
 $\angle 6$ and $\angle 3$ are supp., so $c \parallel d$ by the Conv. of the Same-Side Int. \triangleq Thm.
- $m\angle 1 = 99^\circ$
 $m\angle 7 = (13x + 8)^\circ = 13(7) + 8 = 99^\circ$
 $\angle 1 \cong \angle 7$, so $c \parallel d$ by the Conv. of the Alt. Ext. \triangleq Thm.

LESSON 3-4

- \overline{KM}
- $KM < KL$
 $x - 5 < 8$
 $x < 13$

Statements	Reasons
1. $\overline{AD} \parallel \overline{BC}$, $\overline{AD} \perp \overline{AB}$, $\overline{DC} \perp \overline{BC}$	1. Given
2. $\overline{AB} \perp \overline{BC}$	2. \perp Transv. Thm.
3. $\overline{AB} \parallel \overline{CD}$	3. 2 lines \perp to the same line \rightarrow the two lines are \parallel

SKIP

LESSON 3-5

- Substitute $(-3, 2)$ for (x_1, y_1) and $(4, 1)$ for (x_2, y_2) in the slope formula and then simplify.

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{1 - 2}{4 - (-3)} = \frac{-1}{7} = -\frac{1}{7}$$
- Substitute $(1, 4)$ for (x_1, y_1) and $(-2, -1)$ for (x_2, y_2) in the slope formula and then simplify.

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-1 - 4}{-2 - 1} = \frac{-5}{-3} = \frac{5}{3}$$
- $\text{slope of } \overleftrightarrow{EF} = \frac{4 - 2}{-3 - 8} = \frac{2}{-11} = -\frac{2}{11}$
 $\text{slope of } \overleftrightarrow{GH} = \frac{3 - 1}{-4 - 6} = \frac{2}{-10} = -\frac{1}{5}$
 The slopes are not the same, so the lines are not parallel. The product of the slopes is not -1 , so the lines are not perpendicular.
- $\text{slope of } \overleftrightarrow{JK} = \frac{-2 - 3}{-4 - 4} = \frac{-5}{-8} = \frac{5}{8}$
 $\text{slope of } \overleftrightarrow{LM} = \frac{1 - 6}{-3 - 5} = \frac{-5}{-8} = \frac{5}{8}$
 The lines have the same slope, so they are parallel.
- $\text{slope of } \overleftrightarrow{ST} = \frac{3 - 5}{2 - (-4)} = \frac{-2}{6} = -\frac{1}{3}$
 $\text{slope of } \overleftrightarrow{UV} = \frac{4 - 1}{4 - 3} = 3$
 The product of the slopes is $(-\frac{1}{3})(3) = -1$, so the lines are perpendicular.

LESSON 3-6

- $m = \frac{5 - 1}{-3 - 6} = -\frac{4}{9}$
 $y - y_1 = m(x - x_1)$
 $y - 1 = -\frac{4}{9}(x - 6)$
 $y - 1 = -\frac{4}{9}x + \frac{8}{3}$
 $y = -\frac{4}{9}x + \frac{11}{3}$
- $y - y_1 = m(x - x_1)$
 $y - (-4) = \frac{2}{3}(x - (-3))$
 $y + 4 = \frac{2}{3}(x + 3)$
 $y + 4 = \frac{2}{3}x + 2$
 $y = \frac{2}{3}x - 2$
- $m = \frac{-2 - 0}{0 - 1} = \frac{-2}{-1} = 2$
 $y - y_1 = m(x - x_1)$
 $y - 0 = 2(x - 1)$

33. Solve both equations for y to find the slope-intercept form.

$$\begin{aligned} -3x + 2y &= 5 & 6x - 4y &= 8 \\ 2y &= 3x + 5 & 6x - 8 &= 4y \\ y &= \frac{3}{2}x + \frac{5}{2} & y &= \frac{3}{2}x - 2 \end{aligned}$$

Both lines have a slope of $\frac{3}{2}$, and the y -intercepts are different. So the lines are parallel.

34. Solve the second equation for y to find the slope-intercept form.

$$\begin{aligned} 5x + 2y &= 1 \\ 2y &= -5x + 1 \\ y &= -\frac{5}{2}x + \frac{1}{2} \end{aligned}$$

The lines have different slopes, so they intersect.

35. Solve the second equation for y to find the slope-intercept form.

$$\begin{aligned} 2x - y &= -1 \\ 2x + 1 &= y \\ y &= 2x + 1 \end{aligned}$$

Both lines have a slope of 2 and y -intercept of 1, so they coincide.

CHAPTER TEST, PAGE 206

1. Possible answer: plane $ABC \parallel$ plane DEF

2. Possible answer: $\overline{AC} \parallel \overline{DF}$

3. Possible answer: \overline{AB} and \overline{CF} are skew.

4. $3x + 21 = 4x + 9$

$$21 = x + 9$$

$$12 = x$$

$$3(12) + 21 = 57$$

$$4(12) + 9 = 57$$

Both labeled \sphericalangle

measure 57° .

5. $26x - 7 = 20x + 17$

$$6x - 7 = 17$$

$$6x = 24$$

$$x = 4$$

$$26(4) - 7 = 97$$

$$20(4) + 17 = 97$$

Both labeled \sphericalangle

measure 97° .

6. $42x - 9 = 35x + 12$

$$7x - 9 = 12$$

$$7x = 21$$

$$x = 3$$

$$42(3) - 9 = 117$$

$$35(3) + 12 = 117$$

Both labeled \sphericalangle measure 117° .

7. $m\angle 4 = (16x + 20)^\circ = 16(3) + 20 = 68^\circ$

$$m\angle 5 = (12x + 32)^\circ = 12(3) + 32 = 68^\circ$$

$\angle 4 \cong \angle 5$, so $f \parallel g$ by the Conv. of the Alt. Int. \sphericalangle Thm.

8. $m\angle 3 = (18x + 6)^\circ = 18(4) + 6 = 78^\circ$

$$m\angle 5 = (21x + 18)^\circ = 21(4) + 18 = 102^\circ$$

$$m\angle 3 + m\angle 5 = 78^\circ + 102^\circ = 180^\circ$$

$\angle 3$ and $\angle 5$ are supp., so $f \parallel g$ by the Conv. of the Same-Side Int. \sphericalangle Thm.

9.

Statements	Reasons
1. $\angle 1 \cong \angle 2$, $n \perp \ell$	1. Given
2. $\ell \parallel m$	2. Conv. of the Corr. \sphericalangle Post.
3. $n \perp m$	3. \perp Transv. Thm.

10. Substitute $(-3, -4)$ for (x_1, y_1) and $(-1, 3)$ for (x_2, y_2) in the slope formula and then simplify.

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{3 - (-4)}{-1 - (-3)} = \frac{7}{2}$$

11. Substitute $(-1, -3)$ for (x_1, y_1) and $(2, -1)$ for (x_2, y_2) in the slope formula and then simplify.

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-1 - (-3)}{2 - (-1)} = \frac{0}{5} = 0$$

12. Substitute $(0, -3)$ for (x_1, y_1) and $(5, 1)$ for (x_2, y_2) in the slope formula and then simplify.

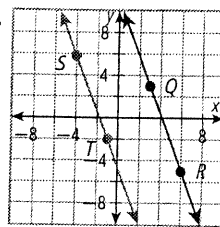
$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{1 - (-3)}{5 - 0} = \frac{4}{5}$$

13. Use the points $(9.5, 0)$ and $(14, 32)$ to graph the line and find the slope.

$$m = \frac{32 - 0}{14 - 9.5} = \frac{32}{4.5} \approx 7.1$$

The slope is about 7.1, which means Greg's average speed was about 7.1 mi/h.

14.



$$\text{slope of } \overleftrightarrow{QR} = \frac{-5 - 4}{6 - 2} = \frac{-9}{4} = -\frac{9}{4}$$

$$\text{slope of } \overleftrightarrow{ST} = \frac{-4 - 5}{-1 - (-4)} = \frac{-9}{3} = -3$$

The lines have the same slope, so they are parallel.

15. $y - y_1 = m(x - x_1)$

$$y - (-5) = -\frac{3}{4}(x - (-2))$$

$$y + 5 = -\frac{3}{4}(x + 2)$$

16. Solve both equations for y to find the slope-intercept form.

$$6x + y = 3$$

$$y = -6x + 3$$

$$2x + 3y = 1$$

$$3y = -2x + 1$$

$$y = -\frac{2}{3}x + \frac{1}{3}$$

The lines have different slopes, so they intersect.