

NOTES: The Quadratic Formula

Date:

x^2 and no x ?

$(x + \#)^2$

$ax^2 + bx + c = 0$

SQUARE ROOTS!

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FACTOR!

Can't factor?

$a \neq 1$
QUADRATIC FORMULA!

$a = 1$
COMPLETE THE SQUARE!

<p>Example: $-16x^2 + 256 = 0$</p> <p>$-256 \quad -256$ $\frac{-16x^2}{-16} = \frac{-256}{-16}$ $\sqrt{x^2} = \sqrt{16}$ $x = \pm 2$</p>	<p>Method: SQUARE ROOTS</p>	<p>Example: $(x - 4)^2 + 5 = 29$</p> <p>$-5 \quad -5$ $\sqrt{(x-4)^2} = \sqrt{24}$ $x - 4 = \pm 2\sqrt{6}$ $+4 \quad +4$</p>	<p>Method: SQUARE ROOTS</p> <p>$x = \pm 2\sqrt{6} + 4$</p>
<p>Example: $x^2 - 10x + 24 = 0$</p> <p>$(x - 6)(x - 4) = 0$</p> <p>$x = 6 \quad x = 4$</p>	<p>Method: FACTOR</p>	<p>Example: $x^2 - 10x - 26 = 0$</p> <p>$x^2 - 10x = 26$ $x^2 - 10x + 25 = 51$ $\sqrt{(x-5)^2} = \sqrt{51}$ $x - 5 = \pm \sqrt{51}$</p> <p>$x = \pm \sqrt{51} + 5$</p>	<p>Method: CAN'T FACTOR! COMPLETE THE SQUARE</p>

The Quadratic Formula: This magic formula will solve ANY QUADRATIC EQUATION. No. Matter. What. When in doubt of which method to use, you can always use the quadratic formula

The standard form of a quadratic equation is $ax^2 + bx + c$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Example 1: The radical will NOT SIMPLIFY	Example 2: The radical WILL SIMPLIFY	Example 3: The radical is a PERFECT SQUARE!
<p>$3x^2 + 5x + 1 = 0$ $a=3$ $b=5$ $c=1$</p> $X = \frac{-5 \pm \sqrt{(5)^2 - 4(3)(1)}}{2(3)}$ $X = \frac{-5 \pm \sqrt{13}}{6}$ <p>NOTHING CAN SIMPLIFY SO OUR ANSWER IS</p> $X = \frac{-5 \pm \sqrt{13}}{6}$	<p>$4x^2 + 4x - 14 = 0$ $a=4$ $b=4$ $c=-14$</p> $X = \frac{-4 \pm \sqrt{(4)^2 - 4(4)(-14)}}{2(4)}$ $X = \frac{-4 \pm \sqrt{240}}{8}$ $X = \frac{-4 \pm 4\sqrt{15}}{8}$ <p>← SIMPLIFY</p> $X = \frac{-1 \pm \sqrt{15}}{2}$ <p>8 CAN DIVIDE INTO -4 AND 4 SO $\frac{-4}{8} = -\frac{1}{2}$</p>	<p>$3x^2 + 5x - 12 = 0$ $a=3$ $b=5$ $c=-12$</p> $X = \frac{-5 \pm \sqrt{(5)^2 - 4(3)(-12)}}{2(3)}$ $X = \frac{-5 \pm \sqrt{169}}{6}$ $X = \frac{-5 \pm 13}{6}$ <div style="display: flex; justify-content: space-around;"> <div style="text-align: center;"> $\frac{-5+13}{6}$ $X = \frac{8}{6}$ </div> <div style="text-align: center;"> $\frac{-5-13}{6}$ $X = \frac{-18}{6}$ </div> </div>